#### **Supplementary Information**

# Theoretical and experimental analysis links isoform-specific ERK signalling to cell fate decisions

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# **Supplementary Tables**

Supplementary Table 1: Relative molar abundances of the non-, mono-, and doublephosphorylated peptide species derived from ERK1 and ERK2 before and after stimulation by Epo determined by UPLC-ESI-MS. The MS ion abundances were converted to relative molar concentrations as described in the text. N.d., not detectable.

peptide	rel. abundance (%) before stimulation	peptide	rel. abundance (%) after stimulation
IADPE-TEY-	100	IADPE-TEY-	63
IADPE-TEpY-	n.d.	IADPE-TEpY-	25
IADPE-pTEpY-	n.d.	IADPE-pTEpY-	12
VADPD-TEY-	97.7	VADPD-TEY-	51
VADPD-TEpY-	2	VADPD-TEpY-	29
VADPD-pTEpY-	0.3	VADPD-pTEpY-	20

Supplementary Table 2: Analysis of additional negative and positive feedback in the model. The nested models were compared to the original model using a likelihood-ratio test.

$\chi^2$	#parameters	p(LRT)
186.569	32	
182.190	36	0.3571
185.981	34	0.7453
185.693	34	0.6456
183.342	36	0.5206
185.868	34	0.7043
185.940	34	0.7302
	χ <sup>2</sup> 186.569 182.190 185.981 185.693 183.342 185.868 185.940	$\chi^2$ #parameters186.56932182.19036185.98134185.69334183.34236185.86834185.94034

### Supplementary figure legends

**Supplementary Figure 1** Ordinary differential equations, parameters, observables, scaling factors and constraints for the mathematical model. Ordinary differential equations (ODE) are shown for the mathematical model of the Epo-induced ERK signalling pathway. Delayed activation of membrane-associated SHP1 was modelled using the linear chain trick approach realised with a 9-step compartmentalisation reaction. Parameters, observables, scaling factors, and constraints are shown with the respective descriptions.

Supplementary Figure 2 Quantitative immunoblotting data of primary erythroid progenitor cells stimulated with erythropoietin. Primary erythroid progenitor cells of the colony-forming unit erythroid stage (CFU-E) were stimulated with 50 U/ml Epo and samples were taken up to 70 min after adding Epo. Cellular lysates were either first subjected to immunoprecipitation (IP) or separated directly (TCL) in a randomised order by SDS-PAGE followed by quantitative immunoblotting (IB). GST-JAK2 and GST-EpoR were added prior to IP acting as calibrators. These calibrators as well as the normalisers  $\beta$ -actin and Clathrin HC were used to normalise the data.

**Supplementary Figure 3** The polyclonal antibodies used in this study do not cross-react with single-phosphorylated MEK/ERK in a way that would have a significant influence on the results. (A) Primary CFU-E cells were stimulated for five different times with 50 U/ml Epo and the cellular lysates were loaded on two gels in triplicates. The first blot was analysed with the polyclonal antibodies that were used in the study, the second blot with monoclonal antibodies that specifically only recognise the double-phosphorylated MEK or the double-phosphorylated ERK. (B) Quantification of the results shows that both types of antibodies result in comparable dynamics of double-phosphorylated MEK2 and double-phosphorylated ERK2. (C) A strong and linear correlation of the results obtained with the polyclonal antibodies is depicted for double-phosphorylated MEK2 and double-phosphorylated ERK2.

**Supplementary Figure 4** Model selection for the plasma membrane module. (A) *Dynamic complex model*: EpoR and JAK2 are modelled being in rapid equilibrium. Gray shading indicates components of biological complexes that were not directly represented in the model Deactivation is modelled by a delayed activation of SHP1. (B) *Stable complex model*: EpoR

and JAK2 are modelled as a stable complex. Deactivation is modelled by a desensitation step. (C) *Stable complex and subcompartment model*: EpoR and JAK2 are modelled as a stable complex. Deactivation is modelled by a desensitation step with a subcompartment of a desensitised, dephosphorylated complex. Process diagram and fits to experimental data are shown. Green shading indicates variables contributing to the observed pJAK2, red shading depicts variables contributing to the observed pEpoR and yellow shading indicates contributions to both.

**Supplementary Figure 5** The dose response of phosphorylated JAK2 and EpoR versus Epo is sigmoidal and can be explained by the *dynamic complex model*. (A) CFU-E cells were stimulated for 7 min with Epo concentrations ranging from 0.1 to 1000 U/ml and the phosphorylated and total amount of JAK2 and EpoR were analysed by quantitative immunoblotting. (B) The immunoblots shown in (A) were quantified and computationally processed. Error bars indicate standard deviations of three biological replicates. (C) Dose response profiles of phosphorylated JAK2 at 7 min were simulated using the *stable complex and subcompartment model* (see Figure 4C) and the *dynamic complex model* (see Figure 4A). Predicted values were scaled to the experimental data.

Supplementary Figure 6 Saturation of the kinases does not explain the observed signalling behaviour and modeling complex formation leads to over-parametrisation. (A) Two additional models (complex processive model and complex distributive model) were created by adding complex formation to the phosphorylation reactions of MEK and ERK. (B) Parameters for the models were estimated (1000 fits with quasi-random start values) and the best fit of each model is depicted (dashed lines). Experimental data are depicted as open circles with error bars indicating standard deviations estimated with a smoothing spline approach as described in materials and methods - mathematical modelling, parameter estimation and simulations. (C) The complex distributive model displays the lowest  $\chi^2$  value, but a log-likelihood ratio test rejects this model compared to the original model (distributive model). The Akaike information criterion (AIC) ranks the distributive model as best.

**Supplementary Figure 7** MAP-kinase activation mechanism is distributive for ERK and processive for MEK. (**A**) The reaction mechanism for the processive MAP-kinase activation model is shown. Parameter estimation was performed 1000 times with randomly generated starting values. (**B**) The reaction mechanism for the distributive MAP-kinase activation model

is shown. Parameter estimation was performed 1000 times with randomly generated starting values. The processive and the distributive model were compared with a log-likelihood ratio test, rejecting the processive model (p-value  $< 10^{-6}$ ).

**Supplementary Figure 8** MS/MS spectra of synthetic ERK phosphopeptides. (A) The MS/MS spectra of three synthetic ERK phosphopeptides and sequence information covering the phosphorylated region are depicted. (B) Reporter fragments for the pT-containing peptides are shown with the neutral loss of phosphoric acid.

**Supplementary Figure 9** Label-free quantification of ERK phosphorylation. (A) Reporter fragments showing the pY immonium ion are depicted for the pY-containing synthetic ERK peptides. (B) UPLC-MS elution order of 4 synthetic analogues of the tryptic ERK2 peptides. The selected ion traces correspond to the  $[M+3H]^{3+}$  ions of the peptides as indicated (m/z 715.3 for -TEY-; m/z 742.0 for -TEpY- and -pTEY-; m/z 768.6 for -pTEpY-). (C) Correction factors for conversion of the measured relative ion intensities of the tryptic ERK2 peptide VADPDHDHTGFLTEYVATR into relative molar abundances. The experimental ion intensity values are divided by the given correction factor for conversion into relative molar abundances.

**Supplementary Figure 10** Iterative rounds of parameter estimation and identifiability testing result in accurate determination of identifiable parameters. Parameters, initial concentrations, and scaling factors are displayed in red for standard deviations larger than 15% and in green for standard deviations equal to or smaller than 15%. For each iterative round, 1000 fits were performed and the mean values and standard deviation of each parameter was calculated on the basis of the best 50% of fits. Non-parametric bootstrap-based identifiability testing with the mean optimal transformation approach (MOTA) revealed dependent parameter doublets, triplets, or quadruplets, indicated by upper case letters (A – F). Dependent parameters were fixed to the value of the best fit and parameter estimation was performed again. After restraining the parameter space to 21 parameters, all parameters could be identified.

**Supplementary Figure 11** Parameter doublets, triplets, and quadruplets analytically dependent as identified with the mean optimal transformation approach (MOTA). Analytically dependent parameters identified by MOTA are shown, with upper case letters corresponding to the dependent parameter doublets, triplets, or quadruplets in Supplementary

Figure 10. Data points (circles) represent the estimated parameter values of the best 500 fits of the specific parameter estimation round. The data points describe a straight line (**D**, **E**, **G**), a hyperbola (**A**, **F**, **I**), a two-dimensional surface (**B**, **C**), or a four-parameter dependency (**H**). In the first two cases (**A**, **D**, **E**, **F**, **G**, **I**), fixing one parameter identifies the second parameter; in the latter two cases (**B**, **C**, **H**), two parameters were fixed.

**Supplementary Figure 12** Kinetics and signal amplification of the mathematical model. (**A**) Trajectories are depicted for all protein states of the dynamic pathway model. Data are shown for the observation period of 70 min after stimulation with Epo. mSHP1 and actSHP1 denotes membrane-localised and active SHP1, respectively. mSOS indicates membrane-localised SOS. (**B**) The time and the number of activated molecules at the maximum for pathway components are determined and signal amplification was calculated.

**Supplementary Figure 13** Sensitivity analysis demonstrates that kinetic parameters control the amplitude of the Epo-induced ERK pathway. (A) Graphical representation of the quantities amplitude, integrated response, peak time, and duration. (B) Control coefficients of kinetic parameters for peak amplitude, integrated response, peak time, and signal duration of double-phosphorylated ERK1 and ERK2 are depicted. Positive control coefficients (shades of red) indicate higher values for the derived system quantities for increasing parameters, while negative control coefficients (shades of blue) indicate decreasing values for the quantities for increasing parameter values. Green fields represent no control. As expected by the summation theorems, the sum for parametric control coefficients equals 0 for peak amplitude and -1 for the other quantities.

**Supplementary Figure 14** Overexpression of ERK1 and ERK2 increases differentiation in primary erythroid progenitor cells. Murine erythroid progenitor cells retrovirally transduced with ERK1, ERK2 or vector control were cultivated in serum-free medium supplemented with 0.5 U/ml Epo for the indicated time. Differentiation was measured by flow cytometry, scoring CD71-negative and Ter119-positive cells. Haemoglobin content was analyzed by flow cytometric staining against haemoglobin alpha. Enhanced differentiation as determined by the appearance of the surface marker Ter119 inversely correlates with reduced expression of haemoglobin alpha. It appears that reduction in cell proliferation and enhanced differentiation shortens the time window for transcription of the haemoglobin alpha gene before the cells eject the nucleus and therefore results in reduced haemoglobin expression.

Ordinary differential equations

JAK2:	$\mathbf{x}_1 = -k_1 \mathbf{x}_1 \mathbf{u} 1 + k_6 \mathbf{x}_{10} \mathbf{x}_{13}$
EpoR:	$\mathbf{x}_{2} = -\mathbf{k}_{2} \mathbf{x}_{2} \mathbf{x}_{10} + \mathbf{k}_{5} \mathbf{x}_{11} \mathbf{x}_{13}$
SHP1:	$\mathbf{x}_3 = -k_3 \mathbf{x}_3 \mathbf{x}_{11} + k_4 \mathbf{x}_{13}$
SOS:	$\mathbf{x}_4 = -k_7 \mathbf{x}_4 \mathbf{x}_{11} + k_8 \mathbf{x}_{14}$
	$+ k_{24} \cdot x_{20}$
Raf:	$\mathbf{x}_{5} = -k_{9}\mathbf{x}_{5}\mathbf{x}_{14} + k_{10}\mathbf{x}_{15}$
MEK2:	$\mathbf{x}_{6} = -\mathbf{k}_{11} \mathbf{x}_{6} \mathbf{x}_{15} + \mathbf{k}_{16} \mathbf{x}_{21}$
MEK1:	$\mathbf{x}_7 = -k_{13} \mathbf{x}_7 \mathbf{x}_{15} + k_{16} \mathbf{x}_{22}$
ERK1:	$\mathbf{x}_{8} = -k_{17} \mathbf{x}_{8} \mathbf{x}_{16} - k_{17} \mathbf{x}_{8} \mathbf{x}_{17}$
	$+ k_{22} \cdot x_{23}$
ERK2:	$\mathbf{x}_{9} = -k_{19} \cdot \mathbf{x}_{9} \cdot \mathbf{x}_{16} - k_{19} \cdot \mathbf{x}_{9} \cdot \mathbf{x}_{17}$
	+ <b>k</b> <sub>22</sub> · <b>x</b> <sub>24</sub>
pJAK2:	$\mathbf{x}_{10} = + \mathbf{k}_1 \mathbf{x}_1 \mathbf{u} 1 - \mathbf{k}_6 \mathbf{x}_{10} \mathbf{x}_{13}$
pEpoR:	$\mathbf{x}_{11} = + \mathbf{k}_2 \mathbf{x}_2 \mathbf{x}_{10} - \mathbf{k}_5 \mathbf{x}_{11} \mathbf{x}_{13}$
mSHP1:	$\mathbf{x}_{12} = + \mathbf{k}_3 \mathbf{x}_3 \mathbf{x}_{11} - \mathbf{k}_3 \mathbf{x}_{12}$
actSHP1:	$\mathbf{x}_{13} = + k_3 \cdot \mathbf{x}_{32} - k_4 \cdot \mathbf{x}_{13}$
mSOS:	$\mathbf{x}_{14} = + k_7 \mathbf{x}_4 \mathbf{x}_{11} - k_8 \mathbf{x}_{14}$
	$-k_{23} \cdot \mathbf{x}_{14} \cdot \mathbf{x}_{18} - k_{23} \cdot \mathbf{x}_{14} \cdot \mathbf{x}_{19}$
pRaf:	$\mathbf{x}_{15} = + \mathbf{k}_9 \mathbf{x}_5 \mathbf{x}_{14} - \mathbf{k}_{10} \mathbf{x}_{15}$
ppMEK2:	$\mathbf{x}_{16} = + k_{12} \mathbf{x}_{21} \mathbf{x}_{15} - k_{15} \mathbf{x}_{16}$
ppMEK1:	$\mathbf{x}_{17} = + \mathbf{k}_{14} \mathbf{x}_{22} \mathbf{x}_{15} - \mathbf{k}_{15} \mathbf{x}_{17}$
ppERK1:	$\mathbf{x}_{18} = + \mathbf{k}_{18} \mathbf{x}_{23} \mathbf{x}_{16} + \mathbf{k}_{18} \mathbf{x}_{23} \mathbf{x}_{17}$
	$-k_{21} \cdot \mathbf{x}_{18}$
ppERK2:	$\mathbf{x}_{19} = + \mathbf{k}_{20} \mathbf{x}_{24} \mathbf{x}_{16} + \mathbf{k}_{20} \mathbf{x}_{24} \mathbf{x}_{17}$
	– <i>k</i> <sub>21</sub> ·x <sub>19</sub>
pSOS:	$\mathbf{x}_{20} = + \mathbf{k}_{23} \mathbf{x}_{14} \mathbf{x}_{18} + \mathbf{k}_{23} \mathbf{x}_{14} \mathbf{x}_{19}$
	$-k_{24} \cdot x_{20}$
pMEK2:	$\mathbf{x}_{21} = + k_{11} \mathbf{x}_6 \mathbf{x}_{15} - k_{12} \mathbf{x}_{21} \mathbf{x}_{15}$
	+ $k_{15} \mathbf{x}_{16} - k_{16} \mathbf{x}_{21}$
pMEK1:	$\mathbf{x}_{22} = + \mathbf{k}_{13} \mathbf{x}_7 \mathbf{x}_{15} - \mathbf{k}_{14} \mathbf{x}_{22} \mathbf{x}_{15}$
	+ $k_{15} x_{17} - k_{16} x_{22}$
pERK1:	$\mathbf{x}_{23} = + \mathbf{k}_{17} \mathbf{x}_8 \mathbf{x}_{16} + \mathbf{k}_{17} \mathbf{x}_8 \mathbf{x}_{17}$
	$-k_{18} \cdot x_{23} \cdot x_{16} - k_{18} \cdot x_{23} \cdot x_{17}$
	+ $k_{21} \mathbf{x}_{18} - k_{22} \mathbf{x}_{23}$
pERK2:	$\mathbf{x}_{24} = + \mathbf{k}_{19} \cdot \mathbf{x}_{9} \cdot \mathbf{x}_{16} + \mathbf{k}_{19} \cdot \mathbf{x}_{9} \cdot \mathbf{x}_{17}$
	$-k_{20} x_{24} x_{16} - k_{20} x_{24} x_{17}$
0.1.5.4	+ $K_{21} \times_{19} - K_{22} \times_{24}$
mSHP1 <sub>delay1</sub> :	$\mathbf{x}_{25} = + k_{3} \cdot \mathbf{x}_{12} - k_{3} \cdot \mathbf{x}_{25}$
mSHP1 <sub>delay2</sub> :	$\mathbf{x}_{26} = + \mathbf{x}_3 \cdot \mathbf{x}_{25} - \mathbf{x}_3 \cdot \mathbf{x}_{26}$
monP1 <sub>delay3</sub> :	$\mathbf{x}_{27} = + \mathbf{K}_3 \cdot \mathbf{x}_{26} - \mathbf{K}_3 \cdot \mathbf{x}_{27}$
mSHP1 <sub>delay4</sub> :	$\mathbf{x}_{28} = + \mathbf{K}_3 \cdot \mathbf{x}_{27} - \mathbf{K}_3 \cdot \mathbf{x}_{28}$
mSHP1 <sub>delay5</sub> :	$\mathbf{x}_{29} = + \mathbf{K}_{3} \cdot \mathbf{x}_{28} - \mathbf{K}_{3} \cdot \mathbf{x}_{29}$
	$\mathbf{x}_{30} = + \mathbf{x}_{3} \cdot \mathbf{x}_{29} - \mathbf{x}_{3} \cdot \mathbf{x}_{30}$
IIISHP1 delay7	$\mathbf{x}_{31} = + \mathbf{x}_3 \cdot \mathbf{x}_{30} - \mathbf{x}_3 \cdot \mathbf{x}_{31}$
monPi <sub>delay8</sub> :	$\mathbf{x}_{32} = + \kappa_3 \cdot \mathbf{x}_{31} - \kappa_3 \cdot \mathbf{x}_{32}$

#### **Parameters**

JAK2 phosphorylation by Epo:	<i>k</i> <sub>1</sub>
EpoR phosphorylation by pJAK2:	$k_2$
SHP1 activation by pEpoR:	<i>k</i> <sub>3</sub>
SHP1 delay:	<b>k</b> 3 <sup>,</sup>
actSHP1 deactivation:	<i>k</i> 4
pEpoR dephosphorylation by actSHP1:	<i>k</i> 5
pJAK2 dephosphorylation by actSHP1:	<i>k</i> <sub>6</sub>
SOS recruitment by pEpoR:	<b>k</b> 7
mSOS release from membrane:	<i>k</i> 8
mSOS induced Raf phosphorylation:	<i>k</i> 9
pRaf dephosphorylation:	<i>k</i> <sub>10</sub>
1 <sup>st</sup> MEK2 phosphorylation by pRaf:	<i>k</i> <sub>11</sub>
2 <sup>nd</sup> MEK2 phosphorylation by pRaf:	<i>k</i> <sub>12</sub>
1 <sup>st</sup> MEK1 phosphorylation by pRaf:	<i>k</i> <sub>13</sub>
2 <sup>nd</sup> MEK1 phosphorylation by pRaf:	<i>k</i> <sub>14</sub>
1 <sup>st</sup> MEK dephosphorylation:	<i>k</i> <sub>15</sub>
2 <sup>nd</sup> MEK dephosphorylation:	<i>k</i> <sub>16</sub>
1 <sup>st</sup> ERK1 phosphorylation by ppMEK:	<b>k</b> 17
2 <sup>nd</sup> ERK1 phosphorylation by ppMEK:	<i>k</i> <sub>18</sub>
1 <sup>st</sup> ERK2 phosphorylation by ppMEK:	<i>k</i> <sub>19</sub>
2 <sup>nd</sup> ERK2 phosphorylation by ppMEK:	<i>k</i> <sub>20</sub>
1 <sup>st</sup> ERK dephosphorylation:	<i>k</i> <sub>21</sub>
2 <sup>nd</sup> ERK dephosphorylation:	k <sub>22</sub>
ppERK neg feedback on mSOS:	<i>k</i> <sub>23</sub>
pSOS dephosphorylation:	<i>k</i> <sub>24</sub>

#### Observables

pEpoR:	$y_1 = s_1 x_{11}$
pJAK2:	$y_2 = s_2 x_{10}$
ppMEK2:	$y_3 = s_3 x_{16}$
ppMEK1:	$y_4 = s_3 x_{17}$
ppERK1:	$y_5 = s_4 x_{18}$
ppERK2:	$y_6 = s_4 x_{19}$
pSOS:	$y_7 = s_5 x_{20}$
SOS + mSOS:	$y_8 = s_5 (x_4 + x_{14})$

#### **Scaling factors**

scale pEpoR:	<i>s</i> 1
scale pJAK2:	<i>s</i> 2
scale ppMEK:	<i>s</i> 3
scale ppERK:	s <sub>4</sub>
scale SOS:	<i>s</i> 5

#### Constraints

pERK1<sub>max</sub> / ERK1<sub>max</sub> = 0.2 pERK2<sub>max</sub> / ERK2<sub>max</sub> = 0.2 ppERK1<sub>max</sub> / ERK1<sub>max</sub> = 0.1 ppERK2<sub>max</sub> / ERK2<sub>max</sub> = 0.1



Supplementary Figure 2, Schilling, Maiwald et al.





Supplementary Figure 3, Schilling, Maiwald et al.

#### A Dynamic complex model



N=236; fitted parameters = 32; total  $\chi^2$  value = 181.3; AIC = 679.1

#### **B** Stable complex model



N=236; fitted parameters = 29; total  $\chi^2$  value = 392.5; AIC = 884.2

### C Stable complex and subcompartment model



N=236; fitted parameters = 30; total  $\chi^2$  value = 191.4; AIC = 685.1

# Supplementary Figure 4, Schilling, Maiwald et al.



Supplementary Figure 5, Schilling, Maiwald et al.



C model		fitted parameters	total $\chi^2$ value	AIC	
	processive model	26	390.8	878.7	
	distributive model	32	181.3	679.1	
	complex processive model	34	266.4	768.1	
	complex distributive model	48	173.6	703.4	

Supplementary Figure 6, Schilling, Maiwald et al.

#### **Processive MAP-kinase activation** Α



24 reactions 28 ODE 26 fitted parameters 236 data points Total  $\chi^2$  value: 390.8 Akaike information criterion (AIC): 878.7

Β **Distributive MAP-kinase activation** 



34 reactions 32 ODE 32 fitted parameters 236 data points Total  $\chi^2$  value: 181.3 Akaike information criterion (AIC): 679.1

Processive MEK activation	[min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]
1 <sup>st</sup> MEK2 phosphorylation by pRaf	4.083
2 <sup>nd</sup> MEK2 phosphorylation by pRaf	318.4
1 <sup>st</sup> MEK1 phosphorylation by pRaf	0.9448
2 <sup>nd</sup> MEK1 phosphorylation by pRaf	858.8
Distributive ERK activation	[min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]
1 <sup>st</sup> FRK1 phosphorylation by ppMFK	0.005
	2.825
2 <sup>nd</sup> ERK1 phosphorylation by ppMEK	2.825 59.72
2 <sup>nd</sup> ERK1 phosphorylation by ppMEK 1 <sup>st</sup> ERK2 phosphorylation by ppMEK	2.825 59.72 2.769
2 <sup>nd</sup> ERK1 phosphorylation by ppMEK 1 <sup>st</sup> ERK2 phosphorylation by ppMEK 2 <sup>nd</sup> ERK2 phosphorylation by ppMEK	2.825 59.72 2.769 53.23

# Supplementary Figure 7, Schilling, Maiwald et al.



Supplementary Figure 8, Schilling, Maiwald et al.



Supplementary Figure 9, Schilling, Maiwald et al.

	32 parameters estimated	ΜΟΤΑ	25 parameters estimated	ΜΟΤΑ	21 parameters estimated	Parameters
JAK2 phosphorylation by Epo [min <sup>-1</sup> (U/ml) <sup>-1</sup> ]	0.01229 ± 0.0002662 (2%)		0.01235 ± 0.000209 (2%)		0.01234 ± 0.0002096 (2%)	0.0122149
EpoR phosphorylation by pJAK2 [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	3.077 ± 0.5756 (19%)		2.968 ± 0.4354 (15%)	G	fixed	3.15714
SHP1 activation by pEpoR [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	0.4116 ± 0.008597 (2%)		0.4091 ± 0.002953 (1%)		0.4093 ± 0.003021 (1%)	0.408408
actSHP1 deactivation [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	0.02363 ± 0.001449 (6%)		0.0246 ± 0.000579 (2%)		0.0243 ± 0.0007702 (3%)	0.0248773
pEpoR dephosphorylation by actSHP1 [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	1.543 ± 1.157 (75%)		1.142 ± 0.162 (14%)	G	1.188 ± 0.02924 (2%)	1.19995
pJAK2 dephosphorylation by actSHP1 [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	0.4798 ± 0.3436 (72%)	Α	0.3681 ± 0.00696 (2%)		0.3657 ± 0.00712 (2%)	0.368384
SOS recruitment by pEpoR[min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	0.09929 ± 0.004602 (5%)		0.09869 ± 0.005082 (5%)		0.1025 ± 0.00847 (8%)	0.10271
mSOS release from membrane [min <sup>-1</sup> ]	11.54 ± 6.049 (52%)		11.34 ± 5.32 (47%)	н	15.43 ± 1.01 (7%)	15.5956
mSOS induced Raf phosphorylation[min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	0.2005 ± 0.1733 (86%)		0.2029 ± 0.1447 (71%)	н	0.1453 ± 0.01783 (12%)	0.144515
pRaf dephosphorylation [min <sup>-1</sup> ]	0.3578 ± 0.01813 (5%)		0.3523 ± 0.01348 (4%)		0.3737 ± 0.003591 (1%)	0.374228
1 <sup>st</sup> MEK2 phosphorylation by pRaf [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	4.083 ± 3.149 (77%)	в	2.884 ± 0.125 (4%)		3.118 ± 0.0313 (1%)	3.11919
2 <sup>nd</sup> MEK2 phosphorylation by pRaf [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	318.4 ± 226.2 (71%)	С	fixed			215.158
1 <sup>st</sup> MEK1 phosphorylation by pRaf [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	0.9448 ± 0.6336 (67%)	в	fixed			0.687193
2 <sup>nd</sup> MEK1 phosphorylation by pRaf [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	858.8 ± 564.8 (66%)	С	597 ± 37.96 (6%)		665.5 ± 10.47 (2%)	667.957
1 <sup>st</sup> MEK dephosphorylation [min <sup>-1</sup> ]	0.143 ± 0.009349 (7%)		0.1437 ± 0.008317 (6%)		0.1317 ± 0.001564 (1%)	0.130937
2 <sup>nd</sup> MEK dephosphorylation [min <sup>-1</sup> ]	0.07794 ± 0.01871 (24%)	В, С	fixed			0.0732724
1 <sup>st</sup> ERK1 phosphorylation by ppMEK [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	2.825 ± 2.035 (72%)	D	fixed			2.4927
2 <sup>nd</sup> ERK1 phosphorylation by ppMEK [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	59.72 ± 41.84 (70%)	Е	59.54 ± 0.1004 (0%)		59.56 ± 0.1582 (0%)	59.5251
1 <sup>st</sup> ERK2 phosphorylation by ppMEK [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	2.769 ± 1.994 (72%)	D	2.443 ± 0.002752 (0%)		2.446 ± 0.003453	2.44361
2 <sup>nd</sup> ERK2 phosphorylation by ppMEK [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	53.23 ± 37.31 (70%)	Е	fixed		(0%)	53.081
1 <sup>st</sup> ERK dephosphorylation [min <sup>-1</sup> ]	58.7 ± 40.72 (69%)		58.75 ± 13.46 (23%)	I I	39.21 ± 0.1427 (0%)	39.088 <b>6</b>
2 <sup>nd</sup> ERK dephosphorylation [min <sup>-1</sup> ]	5.08 ± 3.407 (67%)		4.508 ± 1.027 (23%)	I I	3.016 ± 0.007706 (0%)	3.00453
ppERK neg feedback on mSOS [min <sup>-1</sup> (10 <sup>4</sup> molecules) <sup>-1</sup> ]	5270 ± 2309 (44%)		5064 ± 2025 (40%)	н	fixed	5122.68
pSOS dephosphorylation [min <sup>-1</sup> ]	0.1216 ± 0.005523 (5%)		0.1211 ± 0.005964 (5%)		0.1255 ± 0.01053 (8%)	0.124944
JAK2 [×10 <sup>4</sup> molecules]	determined					2
EpoR [×10 <sup>4</sup> molecules]	determined					1
SHP1 [×10 <sup>4</sup> molecules]	13.09 ± 10.76 (82%)	Α	fixed			10.7991
SOS [×10 <sup>4</sup> molecules]	3.107 ± 2.186 (70%)	F	2.51 ± 0.008011 (0%)		2.509 ± 0.01336 (1%)	2.5101
Raf [×10 <sup>4</sup> molecules]	5.201 ± 4.705 (90%)		5.138 ± 3.97 (77%)	н	fixed	3.7719
MEK2 [×10 <sup>4</sup> molecules]	determined					11
MEK1 [×10 <sup>4</sup> molecules]	determined					24
ERK1 [×10 <sup>4</sup> molecules]	determined					7
ERK2 [×10 <sup>4</sup> molecules]	determined					21
scale pEpoR [×10 <sup>4</sup> molecules/a.u.]	0.4964 ± 0.005524 (1%)		0.4968 ± 0.004462 (1%)		0.4926 ± 0.004916 (1%)	0.493312
scale pJAK2 [×10 <sup>4</sup> molecules/a.u.]	0.21 ± 0.001148 (1%)		0.2096 ± 0.000601 (0%)		0.2097 ± 0.0007172 (0%)	0.21008
scale ppMEK [×10 <sup>4</sup> molecules/a.u.]	28.37 ± 10.24 (36%)		28.13 ± 6.391 (23%)	I	fixed	40.5364
scale ppERK [×10 <sup>4</sup> molecules/a.u.]	13.44 ± 0.09748 (1%)		13.46 ± 0.1056 (1%)		13.64 ± 0.04152 (0%)	13.5981
scale SOS [×10 <sup>4</sup> molecules/a.u.]	1.379 ± 0.9862 (71%)	F	fixed			1.10228
					1	1

Supplementary Figure 10, Schilling, Maiwald et al.



# Supplementary Figure 11, Schilling, Maiwald et al.



# В

	JAK2	Ep	oR	sc	DS	R	af	ME	EK1/2	ERK1/2
time at maximum	8:27 min	3:52	min	1:03	min	1:24	min	6:5	1 min	7:02 min
total molecules	20000	100	000	34100 54800		300	35	0000	280000	
concentration	0.083 µM			0.142 μM		0.227 µM		1.4	53 µM	1.162 µM
activated molecules at maximum	19804	100	000	130		57		5	234	27272
signal amplification	ation ×0.5		×0.	.013 ×0.		).44 ×9		92	×	5

# Supplementary Figure 12, Schilling, Maiwald et al.





В

Α

JAK2 phosphorylation by Epo **EpoR phosphorylation by JAK2** SHP1 activation by pEpoR actSHP1 deactivation pEpoR dephosphorylation by actSHP1 pJAK2 dephosphorylation by actSHP1 SOS recruitment by pEpoR mSOS release from membrane mSOS induced Raf phosphorylation pRaf dephosphorylation 1<sup>st</sup> MEK2 phosphorylation by pRaf 2<sup>nd</sup> MEK2 phosphorylation by pRaf 1<sup>st</sup> MEK1 phosphorylation by pRaf 2<sup>nd</sup> MEK1 phosphorylation by pRaf 1<sup>st</sup> MEK dephosphorylation 2<sup>nd</sup> MEK dephosphorylation 1<sup>st</sup> ERK1 phosphorylation by ppMEK 2<sup>nd</sup> ERK1 phosphorylation by ppMEK 1<sup>st</sup> ERK2 phosphorylation by ppMEK 2<sup>nd</sup> ERK2 phosphorylation by ppMEK 1<sup>st</sup> ERK dephosphorylation 2<sup>nd</sup> ERK dephosphorylation ppERK neg feedback on mSOS pSOS dephosphorylation

Supplementary Figure 13, Schilling, Maiwald et al.



Supplementary Figure 14, Schilling, Maiwald et al.